## Problems on Trains with Solutions - PDF

$18 \mathrm{~km} /$ hour $=5$ metre/second, can be used to convert the speed given in $\mathrm{km} /$ hour to metre/second or vice - versa.
$3 \mathrm{~km} /$ hour $=(3 \times 5 / 18)$ metre/second
and
3 metre/second $=(3 \times 18 / 5) \mathrm{km} / \mathrm{hour}$

## \#2

If a train of length "L" at a speed "v "passes another object of length " $i$ " at a speed x in time "t", then $t=$ time to cross the object $=$ Total Distance $/$ Relative Speed $=L+i / v-x$

- If object is stationary, then $x=0$
- If object is opposite, then put $x=-x$
- and $v-x$ making after is $(v+x)$

A train is said to have crossed an object (stationary or moving) only when the last coach (end) of the train crosses the said object completely. It implies that the total length of the train has crossed the total length of the object.

Hence, the distance covered by the train = length of train + length of object

## Basic Formula

1. Time $=$ Distance $/$ Speed
2. Time to cross an object moving in the direction of train $=$

## Time to cross an object moving in the direction of train

$=$
Length of train + Length of Object Speed of train - Speed of object

| Assume : |
| :--- |
| Length of Train $=L_{t}$ |
| Length of Object $=L$ |
| Speed of Train $=V_{t}=$ time to cross |
| Speed of Object $=V$ |
| Then basic formula can be |
| represented as |
| $\mathbf{t}=\quad \frac{L_{t}+L}{V_{t}-V}$ |

## Important Note

1. If the object is of negligible length, then put length of object, $L=0$ (i.e. tree, man)
2. If the object is stationary, then put speed of object, $\mathrm{V}=0$
3. If the object is moving in opposite direction, then put (-) ve sign before V , so the denominator of the formula becomes

## Different Types of Objects

$$
\begin{aligned}
& V_{t}-(-V)=\left(V_{t}+V\right) \\
& \text { Then } t=\left(L_{t}+L\right)
\end{aligned}
$$

$$
\left(V_{t}+V\right)
$$

| Case | Types of Objects | Time to Cross |
| ---: | :--- | :--- |
| 1. | Object is stationary and <br> is of negligible length e.g. <br> train crosses lamp post, <br> pole, standing man etc, | $t=\frac{\text { Length of Train }}{\text { ppeed of Train }}$ |
| 2. | Object is stationary and <br> is of some length, e.g. <br> train crosses a bridge, $a$ <br> tunnel, platform, or <br> another train at rest | $t=\frac{\text { Length of (Train }+ \text { object) }}{\text { Speed of Train }}$ |
| 3. | Object is moving and is <br> of negligible length, e.g. <br> train crosses a running <br> man, a running car etc. | $t=\frac{\text { Length of Train }}{\text { Speed of (Train-Object) }}$ |
| 4. | Object is moving and has <br> some length, e.g. train <br> crosses another running <br> train | $t=\frac{\text { Length of (Train }+ \text { Object) }}{\text { Speed of (Train-Object) }}$ |

If the object is moving to opposite direction, then denominator becomes speed of (train + object)

## Two Trains Crossing Each Other in Both Directions

Two trains are crossing each other

| Assume: |
| :--- |
| Length of One Train $=L_{1}$ |
| Length of Second Train $=L_{2}$ |
| They are crossing each other in opposite direction <br> in $t_{1}$ seconds |
| They are crossing each other in same direction in |
| $t_{2}$ seconds |
| Then |
| Speed of Faster Train $=\frac{L_{1}+L_{2}}{2}\left[\frac{1}{t_{1}}+\frac{1}{t_{2}}\right]$ |
| Speed of Slower Train $=\frac{L_{1}+L_{2}}{2}\left[\frac{1}{t_{1}}\right.$ |

## APPLICATIONS ON TRAINS.

1. How long will a train 130 m long travelling at 40 km an hour take to pass a kilometer stone?

Solution: $\quad$ Time $=\frac{\text { Total distance }}{\text { Speed }}=\frac{0.130}{40} \mathrm{hr}=\frac{0.130 \times 60 \times 60}{40}=11.7 \mathrm{sec}$.
2. How long will a train 60 m long travelling at 40 km an hour take to pass through a station whose platform is 90 m long?

$$
\begin{aligned}
& \text { Solution: } \quad \text { Speed }=40 \mathrm{~km} / \mathrm{hr}=40 \times \frac{5}{18} \mathrm{~m} / \mathrm{s} \\
& \therefore \quad \text { Time }=\frac{(60+90)}{40 \times 5} \times 18=\frac{150 \times 18}{40 \times 5}=13.5 \text { seconds. }
\end{aligned}
$$

Solution: $\quad 30 \mathrm{~km} / \mathrm{hr}=30 \times \frac{5}{18}=\frac{25}{3} \mathrm{~m} / \mathrm{s}$

4. Find the length of a bridge which a train 130 m long, travelling at 45 km an hour, can cross in 30 secs.

$$
\text { Solution: } \quad 45 \mathrm{~km} / \mathrm{hr}=45 \times \frac{5}{18}=\frac{25}{2}=12.5 \frac{\mathrm{~m}}{\mathrm{~s}}
$$

Distance covered by the train in 30 seconds $=12.5 \times 30=375 \mathrm{~m}$
$\therefore \quad$ Length of bridge $=375-130=245 \mathrm{~m}$.
5. The length of the train that takes 8 seconds to pass a pole when it turns at a $\mathrm{km} / \mathrm{hr}$ is $\qquad$ metres.

Solution: $\quad 36 \mathrm{~km} / \mathrm{hr}=36 \times \frac{5}{18}=10 \mathrm{~m} / \mathrm{s}$
Distance covered by train in 8 seconds= length of train $=8 \times 10=80 \mathrm{~m}$
6. A train 50 metres long passes a platform 100 metres long I 10 seconds. The speed of the train is
$\qquad$ km/hr.

Solution: Speed of train $=\frac{100+50}{10}=15 \mathrm{~m} / \mathrm{s}=\frac{15 \times 18}{5}=54 \mathrm{~km} / \mathrm{hr}$.
7. How many seconds will a train 60 m in length, travelling at the rate of 42 km an hour, take to pass another train 84 m long, proceeding in the same direction at the rate of 30 km an hour?

Solution: Relative Speed $=42-30=12 \mathrm{~km} / \mathrm{hr}=12 \times \frac{5}{18}=\frac{10}{3} \mathrm{~m} / \mathrm{s}$

8. A train 75 metres long overtook a person who was walking at the rate of 6 km an hour, and passed him in $7 \frac{1}{2}$ seconds. Subsequently it overtook a second person, and passed him in $6 \frac{3}{4}$ seconds. At what rate was the second travelling?

Solution: Relative speed of train and the first person $=\frac{75}{\frac{15}{2}}=10 \mathrm{~m} / \mathrm{s}$
$=10 \times \frac{18}{5}=36 \mathrm{~km} / \mathrm{hr}$.
$\therefore$ Speed of train $=36+6=42 \mathrm{~km} / \mathrm{hr}$
Now, relative speed of train and 2 nd person $=\frac{75}{27} \times 4 \mathrm{~m} / \mathrm{s}=\frac{300}{27} \times \frac{18}{5}=40 \mathrm{~km} / \mathrm{hr}$
2. Speed of $2^{\text {nd }}$ person $=42-40=2 \mathrm{~km} / \mathrm{hr}$.

Quicker Maths (Direct Formula): Speed of $2^{\text {nd }}$ person $=$ Relative Speed of train
with respect of 1 st person + Speed of first person - Relative speed of train with respect to $2^{\text {nd }}$ person

$$
=\left(\frac{75}{\frac{15}{2}} \times \frac{18}{5}\right)+6-\left(\frac{75}{27} \times 4 \times \frac{18}{5}\right)=36+6-40=2 \mathrm{~km} / \mathrm{hr}
$$

9. Two trains running at the rates 45 and 36 km an hour respectively, on parallel rails in opposite directions, are observed to pass each other in 8 seconds, and when they are running in the same direction at the same rate as before, a person sitting in the faster train observes that he passes the other in 30 seconds. Find the lengths of the trains.

Solution: Relative Speed of two trains $=45+36=81 \mathrm{~km} / \mathrm{hr}$ (When two train are moving in opposite directions)

$$
\begin{array}{ll}
\quad=81 \times \frac{5}{18}=\frac{45}{2}=22 \frac{1}{2} \mathrm{~m} / \mathrm{s} \\
\therefore \quad & \text { Length of both the trains }=\frac{45}{2} \times 8=180 \mathrm{~m} .
\end{array}
$$

Now, when two trains are moving in the same direction, the relative speed

$$
=45-36=9 \mathrm{~km} / \mathrm{hr}=\frac{9 \times 5}{18}=\frac{5}{2} \mathrm{~m} / \mathrm{s} .
$$

The man sitting in the faster train passes the length of the slower train in 30 seconds.
$\therefore$ Length of the slower train : $=\frac{5}{2} \times 30=75 \mathrm{~m}$.
$\therefore$ Length of the faster train $=180-75=105 \mathrm{~m}$.

## Quicker maths (Direct Formula):

Length of slower train $=30 \times($ Relative speed of two trains $)=30(45-36) \frac{5}{18}=75 \mathrm{~m}$
Length of faster train = Total length of both trains - length of slower train
$=8(45+36) \frac{5}{18}-75$
$=8 \times \frac{81 \times 5}{18}+75=180-75=105 \mathrm{~m}$
10. Two trains measuring 100 m and 80 m respectively, run on parallel lines of rails. When travelling in opposite directions they are observed to pass each other in 9 seconds, but when they are running in the same direction at the rates as before, the faster train passes the other in 18 seconds. Find the speed of the two trains in km per hour.

## Solution: Quicker Maths (Direct Formula):

$R_{1}=$ Relative speed, when they are moving in the same direction

$$
=\frac{100+80}{18}=10 \mathrm{~m} / \mathrm{s}
$$

$\mathrm{R}_{2}=$ Relative Speed, when they are moving in opposite directions

$$
=\frac{100+80}{9}=20 \mathrm{~m} / \mathrm{s}
$$

Speed of faster train $=\frac{R_{1+R_{2}}}{2}=\frac{10+20}{2}=15 \mathrm{~m} / \mathrm{s}$

$$
=15 \times \frac{18}{5}=54 \mathrm{~km} / \mathrm{hr}
$$

Speed of slower train $=\frac{R_{2}-R_{1}}{2}=\frac{20-10}{2}=5 \mathrm{~m} / \mathrm{s}$ $=5 \times \frac{18}{5}=18 \mathrm{~km} / \mathrm{hr}$.

